# Fabrication of single-electron devices using dispersed nanoparticles and fitting the measurement results to curves calculated based on percolation model 

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#### Abstract

We calculated the connection probability , $P_{C}$, between electrodes on the basis of the triangular lattice percolation model for investigating the effect of distance variation between electrodes and the electrode width on fabricated capacitively coupled single-electron transistors. single-electron devices were fabricated via the dispersion of gold nanoparticles (NPs). The NPs were dispersed via the repeated dropping of an NP solution onto a chip. The experimental results were fitted to the calculated results, and the fitting parameters were compared with the occupation probability, $P_{O}$, which was estimated for one drop of the NP solution. On the basis of curves of the drain current vs. the drain-source voltage ( $I_{\mathrm{D}}-V_{\mathrm{DS}}$ ) measured at 77 K , the current was suppressed at approximately 0 V .


Keywords Gold nanoparticle solution • Drop • Percolation

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## 1 Introduction

Single-electron devices has been investigated by many researchers [1] [2]. Single-electron devices have numerous applications including single-electron turnstiles [3], single-electron pumps and high accurate current sources [4] [5] [6] [7] , current mirror [8], single-electron memory [9], a Coulomb blockade thermometer [10], and highly sensitive sensors [11] [12], among others.

The single-electron transistor (SET) is a key singleelectron device [1] [13] . SETs have been fabricated using a combination of electron beam lithography and shadow evaporation [8]. An SET comprises two small tunnel junctions on both sides of an island electrode and a gate electrode. Nanoparticles (NPs) are also used as the island electrode in SETs [14]; however, a special technique is required to fabricate the small nanometerscale gap. Meanwhile, the Coulomb blockade effect has been observed for single-electron devices fabricated via the repeated dispersion of gold NPs and the forming of drain (D) and source (S) electrodes [15].

In this work, we fabricated drain, source, and gate (G) electrodes and fabricated devices by repeatedly dispersing of gold NPs. To disperse the NPs, we dropped a gold NP solution onto a chip on which electrodes had been fabricated.; the we dried the chip. This process of dropping the NP solution and drying was repeated. This method is a simple way to fabricate an NP SET (NP-SET).

## 2 Calculation of connection probability on the basis of percolation theory

When NPs are dispersed, the connection probability $\left(P_{C}\right)$ between the electrodes can be calculated on the


Fig. 1 Schematic of dispersed particles and electrodes on a triangular lattice percolation model. (a) All electrodes are isolated. (b) The source (S) and drain (D) electrodes are connected and the gate (G) electrode is isolated ("S-D_(G)"). (c) The S, D, and G electrodes are connected ("S-D-G").
basis of percolation theory. Fig. 1 shows a schematic of dispersed particles and electrodes. A triangular lattice was used for calculations. When the occupation probability, $P_{O}$, is low, all electrodes are isolated (Fig. 1 (a), $P_{O}=0.15$ ). The area indicated by the arrow is an enlarged view of the region outlined with a dashed line. $G L_{\mathrm{H}}$ and $G L_{\mathrm{V}}$ are the horizontal and vertical grid lengths, respectively. When $P_{O}$ increases, the S and D electrodes are connected and the $G$ electrode is isolated (Fig. 1 (b), $P_{O}=0.4$ ); we refer to this state as " S D_(G)". When $P_{O}$ further increased, not only the S and D electrodes but also the G electrode are connected (Fig. 1 (c), $P_{O}=0.45$ ); we refer to this state as "S-DG". In Fig. 1 (b) and (c), a group of particles that connects the electrodes is denoted by a dashed line. The "S-D_(G)" configuration means that the G electrode couples to the $S$ and $D$ electrodes capacitively. Because the "S-D_(G)" configuration is needed for fabricating a capacitively coupled SET (C-SET), the "S-D_(G)" configuration is very important for the dispersion of the NPs to enable the fabrication of an NP-SET.

The width of each electrode and the length between the electrodes are defined in Fig. 2. The area enclosed by a dashed line is the area used in the calculation based on the triangular lattice percolation model. This area is 200 grids $\times 200$ grids or larger. The width of the source is fixed at 62 grids. $G a p_{\mathrm{S}-\mathrm{D}}, L_{\mathrm{SD}-\mathrm{G}}$, and $W_{\mathrm{G}}$ are the gap length between the source and the drain, the length between the source and the gate, and the width of the gate, respectively.


Fig. 2 Defining the width of each electrode and the length between the electrodes. The area enclosed by a dashed line is that used in calculation based on the triangular lattice percolation model.

The dependence of $P_{C}$ on $P_{O}$ for a $G a p_{\mathrm{S}-\mathrm{D}}$ of 6 grids is shown in Fig. 3 (a). Open circles and filled rectangles show the $P_{C}$ of S-D_(G) and that of S-D-G. $L_{\mathrm{SD}-\mathrm{G}}$ and $W_{\mathrm{G}}$ are 76 grids and 66 grids, respectively. With increasing $P_{O}$, the $P_{C}$ of S-D_(G) increases gradually from a $P_{O}$ of approximately 0.2 to approximately 1.0 at a $P_{O}$ of approximately 0.4 . The notation S-D_(G) means that S and D are connected and that G is isolated, whereas the notation S-D-G means that S, D, and G are connected. Because the $P_{C}$ of S-D-G rapidly increases from a $P_{O}$ of 0.45 to a $P_{C}$ of 1.0 at a $P_{O}$ of 0.5 , the $P_{C}$ of S-D_(G) decreases rapidly from a $P_{O}$ of 0.45 and reaches zero at a $P_{O}$ of 0.5 . This value of $P_{O}(0.5)$ is consistent with the critical probability in the triangular lattice percolation model [17]. With increasing $P_{O}$, the $P_{C}$ of S-D_(G) increases gradually and then decreases rapidly. $P_{C, \text { max }}$ and the full-width of half-maximum (FWHM) are defined as the maximum value of the $P_{C}$ of S-D_(G) and the width of the $P_{C}$ of S-D_(G) at half of $P_{C, \text { MAX }}$, respectively.

Fig. 3 (b) shows the dependence of the $P_{C}$ of SD_(G) $\left(P_{C\left(S-D_{-}(\mathrm{G})\right)}\right)$ on $P_{O}$ for $G^{2} p_{\mathrm{S}-\mathrm{D}}$ of $6,10,14$, and 20 grids. Open circles, triangles, rectangles, and diamonds are data points for $G a p_{S-D}=6,10,14$, and 20 grids, respectively. $L_{\mathrm{SD}-\mathrm{G}}$ and $W_{\mathrm{G}}$ in Fig. 3 (b) are 76 and 66 grids, respectively. With increasing $P_{O}$, the $P_{C,(\mathrm{~S}-\mathrm{D}-(\mathrm{G}))}$ gradually increases from approximately 0.2 , $0.25,0.3$, and 0.38 for $G a p_{\mathrm{S}-\mathrm{D}}$ of $6,10,14$, and 20 grids. For wider $G a p_{\mathrm{S}-\mathrm{D}}$, a larger $P_{O}$ is needed before the $P_{C(\mathrm{~S}-\mathrm{D}-(\mathrm{G}))}$ begins to increase . All of the $P_{C\left(\mathrm{~S}-\mathrm{D}_{-}(\mathrm{G})\right)}$ decrease rapidly from a $P_{O}$ of 0.45 and reach zero at a $P_{O}$ of $0.5 . P_{C, \text { max }}$ and FWHM decrease with increasing $G a p_{S-D}$. The conditions for fabricating a C-SET are preferably adjusted via the dispersion of the NPs such that the maximum value of $P_{C\left(S-D_{-}(\mathrm{G})\right)}$ is high

(a)

(b) S-D_(G)


Fig. 3 The dependence of $P_{C}$ on $P_{O} . L_{\mathrm{SD}-\mathrm{G}}$ and $W_{\mathrm{G}}$ are 76 grids and 66 grids, respectively. (a) $P_{C}$ of S-D_(G) (open circle) and that of S-D-G (filled rectangle) for $G a p_{\mathrm{S}-\mathrm{D}}$ of 6 grids. (b) $P_{C}$ of S-D_(G) for $\operatorname{Gap}_{\mathrm{S}-\mathrm{D}}$ of 6 (circle), 10 (triangle), 14 (rectangle), and 20 grids (diamond).
and the FWHM is wide. Thus, we calculated $P_{C, \text { MAX }}$ and FWHM for various conditions.

Fig. 4 (a), (b), and (c) show the dependence of the $P_{C, \text { MAX }}$ and the FWHM on the $G a p_{\mathrm{S}-\mathrm{D}}, L_{\mathrm{SD}-\mathrm{G}}$, and $W_{\mathrm{G}}$, respectively, where filled symbols indicate the $P_{C, \text { MAX }}$ and open symbols indicate the FWHM. In Fig. 4 (a), $L_{\mathrm{SD}-\mathrm{G}}$ and $W_{\mathrm{G}}$ are 76 and 66 grids, respectively. With increasing $G a p_{\mathrm{S}-\mathrm{D}}$, the $P_{C, \text { max }}$ decreases gradually, but the FWHM decreases rapidly. Thus, a small gap is better for fabricating a C-SET. In Fig. 4 (b), $G a p_{\mathrm{S}-\mathrm{D}}$ and $W_{\mathrm{G}}$ are 6 and 66 grids, respectively. With increasing $L_{\mathrm{SD}-\mathrm{G}}$, the $P_{C, \mathrm{MAX}}$ increases rapidly from 6 to 30 grids of $L_{\mathrm{SD}-\mathrm{G}}$ and reaches approximately 1.0 at 40 grids of $L_{\text {SD-G }}$. The FWHM increases and becomes almost constant when $L_{\text {SD-G }}$ exceeds 40 grids. With respect to the fabrication of SETs, the $L_{\mathrm{SD}-\mathrm{G}}$ is an important parameter for the gate capacitance, $C_{\mathrm{G}}$. A long $L_{\mathrm{SD}-\mathrm{G}}$ makes $C_{\mathrm{G}}$ small and the gate voltage large, resulting in Coulomb oscillation, which is direct evidence of a C-SET. The results in Fig. 4 (b) indicate that 40 grids of $L_{\mathrm{SD}-\mathrm{G}}$ is sufficient. In Fig. 4 (c), the $P_{C, \mathrm{MAX}}$ dependence on $W_{\mathrm{G}}$ is plotted for $L_{\mathrm{SD}-\mathrm{GS}}$ of 6,16 , and 26 grids; the Gap $_{\mathrm{S}-\mathrm{D}}$ is 6 grids. With increasing $L_{\mathrm{SD}-\mathrm{G}}$,


Fig. 4 The dependence of the $P_{C, \text { max }}$ and the FWHM on (a) the $G a p_{\mathrm{S}-\mathrm{D}}$, (b) on the $L_{\mathrm{SD}-\mathrm{G}}$, and (c) on the $W_{\mathrm{G}}$. Filled symbols indicate the $P_{C, \text { max }}$ and open symbols indicate the FWHM. The $L_{\mathrm{SD}-\mathrm{G}}$ and the $W_{\mathrm{G}}$ are 76 and 66 grids in (a), and the $G a p_{\mathrm{S}-\mathrm{D}}$ and the $W_{\mathrm{G}}$ are 6 and 66 grids, respectively in (b). The Gap $p_{\mathrm{S}-\mathrm{D}}$ is 6 grids in (c).
$P_{C, \text { MAX }}$ decreases, starting from approximately 0.6 for an $L_{\mathrm{SD}-\mathrm{G}}$ of 6 , from approximately 1.0 for an $L_{\mathrm{SD}-\mathrm{G}}$ of 16 , and that decreases more slightly from about 1.0 for $L_{\mathrm{SD}-\mathrm{G}}$ of 26 . Thus, $W_{\mathrm{G}}$ is not an effective parameter except in cases where the $L_{\mathrm{SD}-\mathrm{G}}$ is small.

## 3 Experimental details

### 3.1 Fabrication and measurement methods

Four chips (chips A, B, C, and D) were used in the experiments. These chips were covered with an $\mathrm{SiO}_{2}$ layer. The D, S, and G electrodes were fabricated using e-beam lithography (EBL) and shadow evaporation


Fig. 5 An optical micrograph of fabricated electrodes.
[16]. A double layer resist was used for EBL. The bottom layer was $800-\mathrm{nm}$-thick $11 \%$ copolymer, and the top layer was $60-\mathrm{nm}$-thick $2 \%$ PMMA. The accelerating voltage and the beam current were 30 kV and 120 pA, respectively. The area for EBL was square of 200 $\mu \mathrm{m} \times 200 \mu \mathrm{~m}$. After the photo-resist was developing in an isopropanol aqueous solution, resist bridges were formed.

Using shadow evaporation, $20-\mathrm{nm}$-thick gold film was evaporated from an angle of $+14^{\circ}$, and 45 -nm-thick gold film was evaporated from an angle of $-14^{\circ}$. After the photo-resist was lifted off in acetone, 12 gaps between the S and D electrodes were fabricated in an area of $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$. The $L_{\mathrm{SD}-\mathrm{G}}$ was designed to be 1000 nm , whereas the widths of the S and G electrodes were both designed to be 800 nm . Gap $p_{\mathrm{S}-\mathrm{D}}$ was an important parameter in these experiments. The gaps between $S$ and $D$ were fabricated using shadow evaporation, and the resist bridges formed by EBL served used as shadow masks during the evaporation. The $W_{\mathrm{G}}$ was different for each Gap $_{\mathrm{S}-\mathrm{D}}$. The Gap $_{\mathrm{S}-\mathrm{D}}$, and $W_{\mathrm{G}}$ values are summarized in Table. 1.

Table 1 Table of the $G a p_{\mathrm{S}-\mathrm{D}}, W_{\mathrm{G}}$, and the number of gaps for each chip, N .

| Chip | Gap $_{\mathrm{S}-\mathrm{D}} / \mathrm{nm}$ | $W_{\mathrm{G}} / \mathrm{nm}$ | N |
| :--- | :---: | :---: | :---: |
| A, B, C | 300 | 1100 | 3 |
|  | 200 | 1000 | 3 |
|  | 140 | 940 | 3 |
|  | 100 | 900 | 3 |
| D | 140 | 940 | 12 |

An optical micrograph of fabricated electrodes is shown in Fig. 5.

One micro-liter of citric acid gold colloidal solution was dropped onto the chips. The colloidal solution contained 70 ppm of NPs with a diameter of 15 nm . After the dropping procedure, each chip was dried approximately 20 min . The resistance between the S and D electrodes was then measured. A schematic of the resistance measurement circuit is shown in Fig. 6. The


Fig. 6 A schematic of the resistance measuring circuit between the source and the drain. The resistance was measured at room temperature.
resistance was measured at room temperature. Three resisters with a nominal resistance of $1 \mathrm{M} \Omega$ and a circuit tester were used for measuring the resistance. The three resisters were serially connected to the circuit tester, and probes were connected to either side of the middle resistor among the three serially connected resistors. When the probes were connected directly (short circuit), the resistance reading indicated by the circuit tester was $1.98 \mathrm{M} \Omega$. When the probes were placed apart (open circuit), the circuit tester indicated a resistance of $2.97 \mathrm{M} \Omega$. When these two probes were connected to the S and D electrodes, the maximum value of the measurable resistance was approximately $97 \mathrm{M} \Omega$. When the resistance between the S and D electrodes was less than $97 \mathrm{M} \Omega$, we assumed that the gap between the S and D electrodes was bridged by gold NPs. The data for $I_{\mathrm{D}}-V_{\mathrm{DS}}$, where $I_{\mathrm{D}}$ and $V_{\mathrm{DS}}$ are the drain current and voltage between the drain and the source, respectively, were collected using a semiconductor parameter analyzer. The two-probe technique was used for the measurements.

### 3.2 Estimation of the occupation probability per drop

To compare the measured resistance results with the values calculated on the basis of percolation theory, the occupation probability of gold NPs per drop of the gold NP solution was estimated. To estimate the occupation probability, we regarded a droplet dropped onto the chip as a half-sphere. A schematic of a droplet is shown in Fig. 7.

The radius of the half sphere for a droplet of $1 \mu \mathrm{~L}$ is 0.8 mm . Each chip contains 12 gaps, and these gaps exist in a $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$ square area in the center of the chip, whose dimensions are $7 \mathrm{~mm} \times 7 \mathrm{~mm}$. When a droplet is dropped onto the center of a chip, the center of the droplet is the the $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$ square area that contains all the gaps on the chip. This


Fig. 7 A schematic of a droplet to estimate an occupation probability of the dispersed NPs. A droplet dropped onto the chip was regarded as a half-sphere. Radius of the half-sphere for a droplet of $1 \mu \mathrm{~L}$ is 0.8 mm . A bottom area of a square pillar enclosed by a dashed line is $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$ and includes the all gaps on a chip.
square area is shown in Fig. 7 as the bottom layer of a square pillar enclosed by a dashed line. We assumed that NPs included in the square pillar moved down to this area during drying. The specific gravity of the citric acid gold colloidal solution ( pH 6.4 ) was regarded as 1 . The colloidal solution contained 70 ppm NPs with a diameter of 15 nm . This square pillar's bottom area was $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$ and its height is 0.8 mm . The weight of gold included in the square pillar was $2 \times 10^{-9}$ g , and the number of gold NPs with a of diameter of 15 nm in was $6 \times 10^{7}$. For gold NPs of 15 nm in diameter, $G L_{\mathrm{H}}$ and $G L_{\mathrm{V}}$ (Fig. 1) are 15 nm and 13 nm , respectively. The number of NPs needed to occupy the whole area of $200 \mu \mathrm{~m} \times 200 \mu \mathrm{~m}$ on a triangular lattice is $2 \times 10^{8}$. Thus, the occupation probability for one drop is 0.3 . Experimental connection probability values, $P_{C, \mathrm{E}}$, were calculated using the equation for each drop on each chip, $P_{C, \mathrm{E}}=N_{\mathrm{C}} / 12$, where $N_{\mathrm{C}}$ is the number of gaps connected by NPs, and 12 is the total number of gaps on each chip.

In the experiments, after the NP solution was dropped onto the chips, the resistance between the S and D electrodes was measured, whereas that between the $S$ and G electrodes was not measured. For comparison of the resistance measurement results, we calculated $P_{C(S-D)}$ using the following equation,
$P_{C(\mathrm{~S}-\mathrm{D})}=P_{C(\mathrm{~S}-\mathrm{D}-(\mathrm{G}))}+P_{C(\mathrm{~S}-\mathrm{D}-\mathrm{G})}$
where $P_{C\left(\mathrm{~S}-\mathrm{D}_{-}(\mathrm{G})\right)}$ and $P_{C(\mathrm{~S}-\mathrm{D}-\mathrm{G})}$ are the $P_{C}$ of $S-$ $D_{-}(G)$ and that of $S-D-G$, respectively.

The designed values of 1000 nm for $L_{\mathrm{SD}-\mathrm{G}}$ and 800 nm for $W_{\mathrm{S}}$ correspond to 76 and 62 grids, respectively, for a $G L_{\mathrm{V}}$ of 13 nm . The $W_{\mathrm{G}}$ of 66 grids used in the calculation corresponds to 990 nm for a $G L_{\mathrm{H}}$ of 15 nm . The designed gap distances of $100,140,200$, and 300 nm on chips A, B, C, and D correspond to $6,10,14$, and 20 grids, respectively. Because 100, 140, 200, and 300 nm gaps correspond to one-fourth the total number of gaps on Chip A, B, and C, $P_{C, \text { Total }}$ of S-D, $P_{C(S-D)) \text { total }}$ was calculated using the following equation,


Fig. $8 \quad P_{C(S-\mathrm{D})}-P_{O}$ curves. (a) For chip A, B, and C. (b) For chip D. $P_{C(S-D) \text { TOtal }}$ curve calculated by using Eq. 2. By plotting $P_{C, \mathrm{E}}$ on the curve, $P_{O, \mathrm{E}}$ is determined for each $P_{C, \mathrm{E}}$.

$$
\begin{array}{r}
P_{C(\mathrm{~S}-\mathrm{D}) \text { TOTAL }}\left(P_{O}\right)=\left(P_{C(\mathrm{~S}-\mathrm{D}) 6}\left(P_{O}\right)\right. \\
+P_{C(\mathrm{~S}-\mathrm{D}) 10}\left(P_{O}\right)+P_{C(\mathrm{~S}-\mathrm{D}) 14}\left(P_{O}\right) \\
\left.+P_{C(\mathrm{~S}-\mathrm{D}) 20}\left(P_{O}\right)\right) \times 0.25 \tag{2}
\end{array}
$$

where $P_{C(\mathrm{~S}-\mathrm{D}) \mathrm{N}}\left(P_{O}\right)$ is $P_{C(\mathrm{~S}-\mathrm{D}))}$ for $\operatorname{Gap}_{\mathrm{S}-\mathrm{D}}$ of N grids at $P_{O}$.

If we assume that the NPs are fixed on the chip after the $M$ th drop and that NPs occupy vacancies with a probability of $P_{O, I N C R}$ at the $(M+1)$-th drop, the occupation probability can be calculated using the following equations:
$P_{O}(M+1)=P_{O}(M)+\left(1-P_{O}(M)\right) \times P_{O, I N C R}$
$P_{O, I N I T}=P_{O}(1)$
where $P_{O}(M+1)$ and $P_{O}(M)$ are the occupation probabilities at the $(M+1)$-th drop and at the $M$ th drop, respectively.

## 4 Results and Discussion

The $P_{C(S-D) \text { total }}$ curve calculated using Eq. 2 is shown in Fig. 8.

By plotting $P_{C, \mathrm{E}}$ on the curve, we determined the occupation probability based on the results of the resistance measurements, $P_{O, \mathrm{E}}$ for each $P_{C, \mathrm{E}}$.

Table 2 Determined $P_{O, \mathrm{E}}$ for each $P_{C, \mathrm{E}}$ at the $M$ th drop. $" * "$ indicates that the dropping of the NP solution was completed, and "-" indicates that the resistance was not measured. $P_{O, \mathrm{E}}$ was not determined for a $P_{C, \mathrm{E}}$ of 0 ( shown as $" * * * ")$.

| Chip | $P$ | $M$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 |  |
|  | $P_{C, \mathrm{E}}$ | 0.33 | 0.58 | 0.58 | 0.92 | $*$ | $*$ | $*$ |  |
|  | $P_{O, \mathrm{E}}$ | 0.36 | 0.41 | 0.41 | 0.47 | $*$ | $*$ | $*$ |  |
| B | $P_{C, \mathrm{E}}$ | - | 0 | - | 0.17 | - | 0.58 | 0.75 |  |
|  | $P_{O, \mathrm{E}}$ | - | $* * *$ | - | 0.31 | - | 0.41 | 0.44 |  |
| C | $P_{C, \mathrm{E}}$ | 0.50 | 0.42 | 0.50 | 0.17 | 0.58 | $*$ | $*$ |  |
|  | $P_{O, \mathrm{E}}$ | 0.40 | 0.38 | 0.40 | 0.31 | 0.41 | $*$ | $*$ |  |
| D | $P_{C, \mathrm{E}}$ | 0.08 | 0.08 | 0.08 | 0.08 | 0.08 | 0.42 | 0.42 |  |
|  | $P_{O, \mathrm{E}}$ | 0.30 | 0.30 | 0.30 | 0.30 | 0.30 | 0.37 | 0.37 |  |

The $P_{C, \mathrm{E}}$ and the $P_{O, \mathrm{E}}$ at the $M$ th drop on chips $\mathrm{A}, \mathrm{B}, \mathrm{C}$, and D are summarized in Table 2
, where "*" indicates that the dropping of the NP solution was completed, and "-" indicates that the resistance was not measured. $P_{O, \mathrm{E}}$ was not determined for a $P_{C, \mathrm{E}}$ of 0 ( shown as "***") because $P_{O}$ does not have a unique value for a $P_{C, \mathrm{E}}$ of 0 on the $P_{C(S-\mathrm{D}) \text { Total }}$ curve shown in Fig. 8.

For fitting, a combination of $P_{O, I N I T}$ and $P_{O, I N C R}$ was found to minimize the sum of $\left(P_{O}(M)-P_{O, \mathrm{E}}(M)\right)^{2}$, where $P_{O}(M)$ is defined in Eq. 3 and Eq. 4 and $P_{O, \mathrm{E}}(M)$ is $P_{O, \mathrm{E}}$ at the $M$ th drop.

The fitting results for chip A, B, and D are shown in Fig. 9 and the fitting parameters are summarized in Table 3. In the case of chip C, we could not fit the results because the $P_{C}$ decreased at the fourth drop. We cannot explain this decrease of $P_{C}$ on the basis of our two-dimensional percolation model. This decrease may be caused by the breaking of a connection between NPs, when the NP solution was added and some of the NPs changed their position.

Table 3 Table of fitting parameter.

| Chip name | $P_{O, I N I T}$ | $P_{O, I N C R}$ |
| :--- | :---: | :---: |
| Chip A | 0.36 | 0.055 |
| Chip B | 0.14 | 0.070 |
| Chip D | 0.29 | 0.015 |

The $P_{O}$ for one drop was determined to be 0.3. $P_{O}$ for the first drop, $P_{O, I N I T}$ for the chips A, B, and D are $0.36,0.14$, and 0.29 respectively. These values are of the order as the occupation probability for a single drop: 0.3 . However the $P_{O, I N C R}$ values are $0.055,0.070$, and 0.015 for chips A, B, and D, respectively. These values are considerably smaller than 0.3 , which may be caused by residual citric acid in vacancies preventing additional


Fig. 9 Fitting results. Experimental results were fitted by using Eq. 3 and Eq. 4. Fitting parameters are listed in Table 3. (a) Results for chip A and B. $P_{C(S-D) T o t a l}$ was calculated by using Eq. 2. (b) Results for chip D.

NPs from moving into the vacancies. A portion of the NPs may be covered with residual citric acid, which can function as a tunneling barrier.

For chips A and chip B, we collected $I-V$ curves at 77 K for 10 samples. The curves were strongly nonlinear: $G(0 \mathrm{~V}) / G(20 \mathrm{~V})<0.02$, where $G(0 \mathrm{~V})$ and $G(20 \mathrm{~V})$ are the conductance at 0 V and at 20 V , respectively, in the case of the two samples. . However, we could not find specific evidence that these two samples worked as single-electron devices.

Fig. 10 shows $I_{\mathrm{D}}-V_{\mathrm{DS}}$ curves collected at 77 K and at a gate voltage, $V_{\mathrm{G}}$, of 0 V for chip D. Fig. 10 (a) includes two $I_{\mathrm{D}}-V_{\mathrm{DS}}$ curves. These two curves were obtained by consecutive measurements. These two curves do not overlap in the voltage region beyond approximately 0.8 V . Enlarged views of the regions around 0 V and 0.8 V in Fig. 10 (a) are shown in sub-figures (b) and (c), respectively. There is a current suppressed region at approximately 0 V in Fig. 10 (a). In Fig. 10 (b), the first and second $I_{\mathrm{D}}$ values overlap; however in Fig. 10 (c) those $I_{\mathrm{D}}$ values do not overlap in the region beyond approximately 0.8 V . This mismatch may be caused by charging or by a positional shift of the NPs. Because of these current-suppression effects and the mismatch, we speculate that this sample functioned as a singleelectron device. $I-V$ curves collected under various applied gate voltages may be discussed in elsewhere.
(a)

(b)

(c)


Fig. $10 \quad I_{\mathrm{D}}-V_{\mathrm{DS}}$ curves collected at 77 K and at a gate voltage, $V_{\mathrm{G}}$, of 0 V for chip D . These curves were obtained by consecutive measurements. The first and second $I_{\mathrm{D}}$ are plotted as filled circle and open square, respectivly. (a) Whole view. (b) Enlarged view of the regions around 0 V enclosed by a dot-and-dash line in (a). (c) Enlarged view of the regions around 0.8 V enclosed by a dashed line in (a).

## 5 Conclusion

We have calculated the connection probability $P_{C}$ between the S and D electrodes on the basis of the triangular lattice percolation model to investigate effects of varying the length between electrodes and the width of electrode for fabricating capacitively coupled singleelectron transistors. Varying the gap length between the $S$ and $D$ electrodes and also that between the $S$ and G electrodes was effective. Single-electron devices were fabricated via the dispersion of gold NPs. We dispersed the gold NPs by repeatedly dropping a gold NP solution onto a chip, followed by drying the chip. We measured the resistance between the S and D electrodes. To compare the calculated calculated results with the experimental results, we defined $P_{C, \mathrm{E}}$ on the basis of resistance measurements and subsequently fitted the results to the calculated $P_{C, \mathrm{E}}$ values. The $P_{O}$ per drop was estimated to be 0.3 and was the same order for the first drop; however, the $P_{O}$ was small after second drop. On the basis of $I_{\mathrm{D}}-V_{\mathrm{DS}}$ curves collected at 77 K , the current was suppressed at approximately 0 V .

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